

# NOVEL MODELLING AND NUMERICAL APPROACHES FOR FLOW AND TRANSPORT PROCESSES IN POROUS MEDIA TRACK NUMBER 600

MARCO BERARDI\*, MARIO PUTTI§, MATTEO ICARDI† AND BAGUS MULJADI†

\* Consiglio Nazionale delle Ricerche  
Istituto di Ricerca sulle Acque, via F. De Blasio 5, 70132, Bari, Italy  
marco.berardi@ba.irsra.cnr.it

§ Università degli Studi di Padova,  
Dipartimento di Matematica, Via Trieste 63, 35131 Padova, Italy,  
putti@math.unipd.it

† University of Nottingham  
GeoEnergy Research Centre, University Park, NG7 2RD, Nottingham, UK  
matteo.icardi@nottingham.ac.uk

**Key words:** Fluid Dynamics, Porous Media, Numerical Methods, Multiscale

## ABSTRACT

Porous media are ubiquitous in many industrial and natural processes, and there is a growing need of understanding and predicting the multiscale flow and transport phenomena in key energy and manufacturing sectors such as subsurface reservoirs, vadose and root zones, composite materials, filtration, and catalytic reactors, just to name a few.

Specific challenges in geological media, include heterogeneities at all scales, discontinuities, while they share other modelling difficulties with engineered porous media, such as complex evolving structures, non-stationary and non-equilibrium dynamics, ill-posed calibration and validation, coupling with multi-phase, thermal and mechanical processes.

To tackle these challenges, we advocate a renewed effort in developing flexible modelling and numerical approaches, capable of describing effectively and solving coupled systems of Partial Differential Equations in complex and heterogeneous domains. These include extensions of the classical analytical techniques, such as *Volume Averaging* and *Homogenisation*; specific methods to tackle discontinuities, non-linearities, high-frequency applications; as well as numerical methods such as *Virtual Elements*, *Multiscale Finite Elements and Volumes*, naturally well-suited for some these challenges.

In this minisymposium, we bring together Applied and Numerical Mathematicians, Physicists, Chemical, Petroleum, and Environmental Engineers, Hydrogeologists, to discuss the wider applicability and relevance of mathematical and modelling techniques, and to transfer and bring new ideas into the traditional porous media community.

---

## REFERENCES

- [1] Abreu, E., Bustos, A. and Ferraz, P. and Lambert, W., A Relaxation Projection Analytical Numerical Approach in Hysteretic Two-Phase Flows in Porous Media. *J. Sci. Comput.* (2019) **79**:1936-1980.
- [2] Berardi, M., Difonzo, F. and Vurro, M. and Lopez, L., The 1D Richards' equation in two layered soils: a Filippov approach to treat discontinuities. *Adv Water Resour.* (2018) **115**:264–272.
- [3] Cangiani, A. and Chatzipantelidis, P. and Diwan, G. and Georgoulis, E.H., Virtual Element Method for Quasilinear Elliptic Problems. *arXiv preprint* (2017) arXiv:1707.01592.
- [4] Facca, E. and Cardin, F. and Putti, M., Towards a stationary Monge-Kantorovich dynamics: The physarum polycephalum experience. *SIAM J. Appl. Math.* (2018) **78**:651–676.
- [5] Dentz, M. and Hidalgo, J. and Icardi, M., Mechanisms of Dispersion in Porous Media. *J. Fluid Mech.* (2018). DOI: 10.1017/jfm.2018.120
- [6] Icardi, M. and Niasar V., and Schreyer L., Coupled processes in charged porous media - from theory to applications, *Transport Porous Med.* (2019). DOI: 10.1007/s11242-019-01257-3
- [7] Maggi, F. and Porporato, A., Coupled moisture and microbial dynamics in unsaturated soils. *Water Resour. Res.*, (2008) 43, W07444.
- [8] Muljadi, B.P. and Narski, J. and Lozinski, A. and Degond, P., Nonconforming multiscale finite element method for stokes flows in heterogeneous media. Part I: methodologies and numerical experiments. *Multiscale Model Simul.*, (2015) 13(4), pp.1146-1172.
- [9] Seus, D. and Mitra, K. and Pop, I. S. and Radu, F. A. and Rohde, C., A linear domain decomposition method for partially saturated flow in porous media. *Comput. Methods Appl. Mech. Eng.* (2018) **333**: 331–355.
- [10] Vacca, G., An H1-conforming virtual element for Darcy and Brinkman equations. *Math. Models Methods Appl. Sci.* (2018) **01**:159–194.
- [11] Zakerzadeh, R. and Zunino, P. A computational framework for fluid-porous structure interaction with large structural deformation. *Meccanica* (2019) **54**:101-121.